Ternary Excess Molar Enthalpies of Alcohols with Methyl *t***-Butyl Ether at** *T***=298.15K**

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Ternary excess molar enthalpies H_{m}^{E} at 298.15 K and atmospheric pressure measured in a flow microcalorimeter are reported for the methanol+2-propanol+methyl *t*-butyl ether (MTBE) and ethanol+1-propanol+MTBE systems. The ternary results have been correlated by means of a polynomial equation and used to construct constant excess enthalpy contours. Furthermore, the results have been compared with those calculated from a UNIQUAC associated-solution model taking into account molecular association of alcohols and solvation between unlike alcohols and alcohols with MTBE using only binary information.

KEY WORDS: alcohols; association; excess molar enthalpies; flowcalorimeter; MTBE; solvation.

1. INTRODUCTION

The compositions of reformulated gasoline have received much attention by the Reformulated Gasoline Program of the United States, and stringent requirements have been placed on ozone-forming and air toxic emissions. These goals are achieved today by the addition of oxygenates such as light alcohols and aliphatic branched ethers because of their octane-enhancing and expected air pollution-reducing capabilities.

Methyl *t*-butyl ether (MTBE) as an octane enhancer in gasoline has been widely used over the last 10 years mostly as the result of the mandatory reduction in the use of organometal (e.g., tetra-ethyl lead, tetra-methyl lead, and methyl cyclopentadienyl manganese tricarbonyl) and aromatic compounds (e.g., benzene, toluene, xylenes, and ethylbenzene) in gasoline.

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MTBE is chiefly used as a motor fuel component because of its excellent blending octane number properties. It has outstanding physical properties such as low volatility, miscibility in gasoline, and storage stability. In addition to these properties, MTBE utilization offers ecological advantages, as it reduces the polluting components in exhaust gases such as CO, unburned hydrocarbon, ground-level ozone, and polynuclear aromatics. The economic advantages of the MTBE manufacturing process include lower investment [1], lower operating costs and energy consumption, besides its noteworthy octane properties. From the technological, ecological, and economical point of view, the need for information on the thermodynamic behavior of the liquid mixtures is significantly increasing, and an enormous amount of work [2–7] has been carried out to determine the mixing properties of the oxygenated additive. A reliable knowledge of thermodynamic excess properties for the additive is useful in the blending and refinery process.

We have undertaken a program on the measurements of the thermodynamic properties of ternary blends of oxygenated compounds such as two alcohols and an aliphatic branched ether. In this work, we have measured the ternary excess molar enthalpies of the methanol $+2$ -propanol +MTBE and ethanol+1-propanol+MTBE systems at 298.15 K. Results for the corresponding six constituent binaries of the above two ternary systems at 298.15 K have already been reported: (methanol+2-propanol) [8], (methanol+MTBE) [9], (ethanol+1-propanol) [10], (ethanol+ MTBE) [11], (1-propanol+MTBE) [12], and (2-propanol+MTBE) [12].

2. EXPERIMENTAL

The chemicals and their specifications are listed in Table I. The purities of the compounds analyzed by gas chromatography were of good

			Density $(g \cdot cm^{-3})$		
Chemical	Supplier	Specification $(mol\%)$	Expt.	Lit.	
Methanol	Wako Pure Chemical	G.C.: > 99.7	0.78665	0.78665 [7]	
Ethanol		G.C.: > 99.5	0.78524	0.78530 [13]	
1-Propanol		G.C.: > 99.5	0.79973	0.79975 [14]	
2-Propanol		G.C.: > 99.5	0.78123	0.78129 [14]	
MTBE	Kanto Chemical	G.C.: > 99.0	0.73538	0.73540 [15]	

Table I. Specification and Density *(*g *·* cm*−3)* of the Chemicals at 298.15 K

quality for the excess molar enthalpy measurements. The densities measured by a DMA 58 digital densimeter are in reasonable agreement with literature values [7, 13–15]. Liquids were stored in sealed dark bottles dried over molecular sieves (3A 1/16, 4A 1/16) for about 3 weeks before measurements to eliminate residual traces of water and avoid moisturizing. Just prior to use, the required amount of liquids was degassed for 10 min at about 298.15 K in an ultrasonic bath. During each experimental run the temperature was controlled by a thermostatic water bath within ± 0.005 K. Excess molar enthalpies were determined by a flow microcalorimeter at 298.15 K. Details of the equipment and its operation were described previously [16]. Calibration of the calorimeter was carried out using test mixtures of (benzene+cyclohexane), and our results agreed with literature data [17, 18] to within 5 J *·*mol *−1*.

Ternary mixtures of the methanol+2-propanol+MTBE or ethanol+ 1-propanol+MTBE systems were prepared by mixing the binary mixtures of methanol $(1) + 2$ -propanol (2) or ethanol $(1) + 1$ -propanol (2) with MTBE. The compositions of three binary mixtures corresponding to A, B, and C in Fig. 1 were 25, 50, and 75 mol% of component 1 to cover complete composition ranges of the ternary mixtures. Consider 1 mol of a ternary mixture D prepared by mixing $(1 - x_3)$ mol of binary mixture A and x_3 mole of component 3 (MTBE). The excess enthalpy for a mol of a

Fig. 1. Experimental procedure for the ternary system. A, B, and C correspond to compositions of binary mixture $(1+2)$. D represents a composition of ternary mixture at which measurements were made.

ternary mixture of composition x_1 , x_2 , and x_3 , corresponding to point D shown in Fig. 1, can be expressed as follows:

$$
H_{\text{m, 123}}^{\text{E}} = \Delta H_{\text{m}}^{\text{E}} + (1 - x_3)_D H_{\text{m}, A}^{\text{E}} \tag{1}
$$

where $H_{\text{m, 123}}^{\text{E}}$ is the excess enthalpy per mol of ternary mixture D, and $\Delta H_{\text{m}}^{\text{E}}$ is the excess enthalpy measured for the pseudobinary mixture, which is obtained by mixing the binary mixture A with component 3. $H_{m,A}^E$ is the excess enthalpy for the binary mixture A, whose value at a specified composition was interpolated by means of a spline-fit method. The same holds true with mixtures B and C as in mixture A.

3. RESULTS AND DISCUSSION

Experimental results for $\Delta H_{\text{m}}^{\text{E}}$ and the ternary excess molar enthalpies $H_{m, 123}^E$ are summarized in Table II for the (methanol+2-propanol+ MTBE) system and in Table III for the (ethanol+1-propanol+MTBE) system. The measured values of the ternary mixtures were correlated using the following equation:

$$
H_{\mathrm{m},123}^{\mathrm{E}} = H_{\mathrm{m},12}^{\mathrm{E}} + H_{\mathrm{m},13}^{\mathrm{E}} + H_{\mathrm{m},23}^{\mathrm{E}} + x_1 x_2 x_3 A_{123} / RT \tag{2}
$$

where $H_{m, ij}^E$ were fitted to a polynomial equation of the form

$$
H_{m,ij}^{E}/(J \cdot mol^{-1}) = x_i x_j \sum_{n=1}^{p} a_n (x_i - x_j)^{n-1}
$$
 (3)

where a_n is the coefficient calculated by using an unweighted least-squares method. The values of the coefficients for the six binary mixtures are listed in Table IV along with the standard deviations *s* defined by the formula $s = \left\{ \sum_{i=1}^{m} (H_{\text{exp}}^{E} - H_{\text{cal}}^{E})^{2}/(m-p) \right\}^{0.5}$, where *m* is the number of experimental data points and *p* is the number of parameters. The term Δ_{123} of Eq. (2) is expressed by

$$
\Delta_{123}/RT = \sum_{j=1}^{P} b_j (1 - 2x_3)^{j-1} / \{1 - k(1 - 2x_3)\}\tag{4}
$$

The values of the coefficients b_j and k , the absolute arithmetic-mean deviations $\delta(H_m^E) = \sum_{i=1}^m |H_{\text{exp}}^E - H_{\text{cal}}^E|/m$, and the standard deviations, *s* obtained in fitting Eqs. (3) and (4) to the experimental ternary $H_{m, 123}^E$ are listed in Table V. Constant $H_{m, 123}^E$ contours are plotted in Fig. 2 for the (methanol

 \mathbf{K}^a

"Ternary mixtures were prepared by mixing pure MTBE with [x'_1 methanol + $(1 - x'_1)$ 2-propanol]. Ternary mixtures were prepared by mixing pure MTBE with [*x*−*1* methanol+*(1 − x*−*1)* 2-propanol].

"Ternary mixtures were prepared by mixing pure MTBE with $[x'_1$ ethanol + $(1 - x'_1)$ 1-propanol]. Ternary mixtures were prepared by mixing pure MTBE with [*x*−*1* ethanol+*(1 − x*−*1)* 1-propanol].

Mixture	a ₁	a ₂	a ₃	a_4	s (J·mol ⁻¹)
Methanol + 2-propanol ^a	-302.63	125.72	-8.07	1.05	0.0
$Method + MTBEb$	1152.20	-929.30	55.30	-635.10	1.8
Ethanol + 1-propanol ^{c}	76.72	11 34	8.69	-1.58	0.1
Ethanol + $MTBE^d$	1947.30	-901.61	578.29	-760.01	4.3
1 -Propanol + MTBE ^{e}	2136.60	-1007.80	361.70	-372.20	1.1
2 -Propanol + MTBE ^{e}	3106.10	-914.70	598.40	-629.70	3.4

Table IV. Coefficients of Eq. (3) and Standard Deviations,*s*

^a From Ref. 8.

^b From Ref. 9.

^c From Ref. 10.

^d From Ref. 11.

^e From Ref. 12.

Fig. 2. Contours of excess molar enthalpies for the ternary mixture of methanol+2-propanol+MTBE at 298.15 K. (——) Calculated from Eqs. (3) and (4).

Table V. Coefficients of Eq. (4). Absolute Arithmetic-Mean Deviations, $\delta(H^E_n)$, and Standard Deviations, s **Table V.** Coefficients of Eq. (4), Absolute Arithmetic-Mean Deviations, *d(H*Em*)*, and Standard Deviations,*s*

Fig. 3. Contours of excess molar enthalpies for the ternary mixture of ethanol + 1-propanol + MTBE at 298.15 K. $(___\)$ Calculated from Eqs. (3) and (4).

 $+2$ -propanol + MTBE) system and in Fig. 3 for the (ethanol + 1-propanol + MTBE) system using Eqs. (3) and (4).

Figure 4 shows the plot of the binary excess molar enthalpy H_{m}^{E} against the mole fraction of pure alcohol (x_1) for the six constituent binaries: methanol $(1) + 2$ -propanol (2) , methanol $(1) + MTBE$ (2) , 2-propanol $(1) + MTBE$ (2) , ethanol $(1) + 1$ -propanol (2) , ethanol $(1) + MTBE$ (2), and 1-propanol $(1) + MTBE$ (2). The measured values of pseudobinary excess molar enthalpies $\Delta H_{\text{m}}^{\text{E}}$ are plotted in Fig. 5 for the (methanol+ 2 -propanol + MTBE) system and in Fig. 6 for the (ethanol + 1-propanol+MTBE) system as a function of the mole fraction of MTBE. The experimental pseudobinary excess molar enthalpies are positive for all the studied systems over the whole range of composition. The measured $\Delta H_{\text{m}}^{\text{E}}$ data may be interpreted qualitatively by postulating that the excess molar enthalpy is the result of two opposing effects:

(i) The positive contribution to $\Delta H_{\text{m}}^{\text{E}}$ arises from the breaking, or stretching, of hydrogen bonds in the self-associated alkanol multimers due to the hydroxy groups.

Fig. 4. Excess molar enthalpies H_m^E for the six binary mixtures at 298.15 K: (A) 2-propanol + MTBE, (O) 1-propanol + MTBE, (\Box) ethanol + MTBE, (\bullet) methanol + MTBE, (\triangleleft) ethanol + 1-propanol, and (\blacksquare) methanol + 2-propanol. *(···)* Obtained from the model.

(ii) The negative contribution to $\Delta H_{\text{m}}^{\text{E}}$ arises from the cross-association between unlike alkanol multimers and the solvation between alkanol multimers and MTBE through hydrogen bonding.

The positive experimental results for both systems suggest generally that the hydrogen bonds of the alkanol multimers broken by the addition of MTBE predominate over the weak hydrogen bonds formed between alkanol multimers and sterically hindered MTBE molecules.

4. EXCESS ENTHALPY PREDICTION

The experimental determination of multicomponent properties is considerably more tedious and complicated compared to that of binaries if the

Fig. 5. Excess molar enthalpies $\Delta H_{\text{m}}^{\text{E}}$ for the pseudobinary mixtures of [(methanol+2-propanol)+MTBE] at 298.15 K: $(\blacksquare) x'_1 = 0.25$, $(\blacktriangle) x'_1 = 0.50$, and $(●) x'_1 = 0.75$. $(···)$ Obtained from the model.

data have to be known at any composition. For this reason a practical method of predicting the thermodynamic properties of multicomponent systems from binary data has been proposed. We use a UNIQUAC associated-solution model [19] to express the ternary excess molar enthalpies of the mixtures containing two alcohols and an active nonassociating component.

A and B stand for two alcohols (methanol and 2-propanol or ethanol and 1-propanol) and C denotes methyl *t*-butyl ether (MTBE) as an active nonassociating component. The model assumes that the two alcohols A and B undergo self- and cross-association and solvation with C to form linear complexes: A_i , B_j , $(A_iB_j)_k$, $(B_iA_j)_k$, $A_i(B_jA_k)_l$, $B_i(A_jB_k)$, A_iC , B_iC , $(A_iB_j)_k C$, $A_i(B_iA_k)_l C$, $(B_iA_j)_k C$, and $B_i(A_jB_k) C$, where i, j, k, and l go from 1 to ∞ . Further assumptions are that the association constants of

Mole fraction of MTBE

Fig. 6. Excess molar enthalpies $\Delta H_{\text{m}}^{\text{E}}$ for the pseudobinary mixtures of [(ethanol+1-propanol)+MTBE] at 298.15 K: $(\blacksquare) x_1' = 0.25$, $(\blacktriangle) x_1' = 0.50$, and $(●) x'_1 = 0.75$. $(···)$ Obtained from the model.

the alcohols are independent of the degree of association and the solvation constants are also not concerned with the degree of association and solvation. Thus, the model includes a total of five equilibrium constants: K_A , K_B , K_{AB} , K_{AC} , and K_{BC} . The equilibrium constants of the preceding chemical complex forming reactions are defined in terms of the segment fractions and the molecular geometric volume parameters of the chemical species so that the equilibrium constants are dimensionless.

The model gives the ternary excess molar enthalpy for the systems as the sum of the chemical and physical contribution terms:

$$
H^{\rm E} = H^{\rm E}_{\rm chem} + H^{\rm E}_{\rm phys} \tag{5}
$$

The chemical contribution term is related to the enthalpy of complex formation in the mixing system whose derivation was presented previously

[19]. The physical contribution term is derived by applying the Gibbs– Helmholtz relation to the residual term of the UNIQUAC equation [20]. The association constants of alcohols A and B expressed as K_A and K_B at 323.15 K taken from Ref. 21 are 173.9 for methanol, 110.4 for ethanol, 87.0 for 1-propanol, and 49.1 for 2-propanol. The enthalpy of H-bonding formation is assumed to be $h_A = h_B = h_{AB} = -23.2 \text{ kJ} \cdot \text{mol}^{-1}$ for all alcohols [22], and the enthalpy of complex formation between alcohols and MTBE is estimated as −19.5 kJ·mol⁻¹. Table VI summarizes the solvation constants [23] and enthalpies of complex formation between unlike molecules. The temperature dependence of the equilibrium constants is fixed by the van't Hoff relation and the enthalpies of chemical complex formation are assumed to be independent of temperature. The equilibrium constants at 298.15 K required for the excess enthalpy calculation were obtained according to the van't Hoff equation. The structural parameters of complexes are expressed as the sum of parameters of each monomer. The monomer structural parameters, r and q , were calculated using the method of Vera et al. [24]. In fitting the model to binary H_{m}^{E} data, from a practical point of view the energy parameters a_{ij} in $H_{\text{phys}}^{\text{E}}$ are assumed to be a linear function of temperature as given by $a_{ii}/R = C_{ii} + D_{ii}$ {(T/K) *− 273.15}*. The coefficients *Cij* and *Dij* were obtained by minimizing the sum of squares between the experimental H_{m}^{E} and the values calculated by using the model of a simplex method [25]. The binary parameters and the absolute arithmetic-mean deviations $\delta(H_m^E)$ between the binary experimental and the calculated values are given in Table VII. The model with the association and solvation constants and binary parameters alone was used to predict the ternary excess molar enthalpies. The absolute arithmeticmean deviations of the excess molar enthalpies between the experimental and the calculated values were $11.2 \text{ J} \cdot \text{mol}^{-1}$ for the methanol+

$K_{AB}(T)$	$-h_{AB}$ (kJ·mol ⁻¹)	T(K)
70.0	23.2	323.15
22.0	19.5	298.15
49.0	23.2	323.15
18.0	19.5	298.15
6.0	19.5	298.15
5.0	19.5	298.15

Table VI. Values of Solvation Constants and Enthalpies of Complex Formation Between Unlike Molecules

^a From Ref. 23.

^b From this work.

Mixture $(A + B)$	No. of data points	C_{BA} (K)	C_{AB} (K)	$D_{\rm BA}$	D_{AB}	$\delta(H_{\rm m}^{\rm E})$ $(J \cdot mol^{-1})$
Methanol + 2-propanol ^a	9	-68.29	-293.12	-0.3051	-1.0499	2.2
$Method + MTBEb$	14	-95.19	37197	-0.0301	0.1757	2.5
Ethanol + 1-propanol ^a	15	259.75	193.98	0.9548	0.7018	0.2
$Ethanol + MTBEb$	19	839.30	515.83	2.6866	0.7471	3.2
1-Propanol + $MTBE^b$	18	264.91	377.01	0.7462	0.7250	5.4
2 -Propanol + MTBE ^b	18	283.78	316.54	0.6814	0.3358	3.9

Table VII. Binary Parameters and Absolute Arithmetic-Mean Deviations

^a From Ref. 23.

^b From this work.

2-propanol+MTBE system and 14.7 J⋅mol⁻¹ for the ethanol+1-propanol+MTBE system.

5. CONCLUSION

Ternary excess molar enthalpies have been determined for the metha $nol+2$ -propanol + MTBE and ethanol + 1-propanol + MTBE systems at 298.15 K, and the results compare well with those calculated by using a polynomial equation. Furthermore, the experimental results were represented satisfactorily by the UNIQUAC associated-solution model using only binary parameters.

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